

Evaluate the indicated limits.

1. $\lim_{x \rightarrow 2} \frac{x-2}{\sqrt{2+x}}$
2. $\lim_{x \rightarrow 1} \frac{x^3-1}{x-1}$
3. $\lim_{x \rightarrow 1} \left[\frac{1}{1-x} - \frac{3}{1-x^2} \right]$
4. $\lim_{x \rightarrow 0} \frac{\csc x - \cot x}{x}$
5. $\lim_{x \rightarrow 0} \frac{\sin ax}{\sin bx}$
6. $\lim_{x \rightarrow 0} x \sin \left(\frac{1}{x} \right)$
7. $\lim_{x \rightarrow 0} \frac{1-\cos x}{x}$
8. $\lim_{y \rightarrow x} \frac{y^{2/3} - x^{2/3}}{y-x}$
9. $\lim_{x \rightarrow \pi} \frac{\tan(\sin x)}{\sin x}$
10. $\lim_{x \rightarrow 0} \text{Sin} \left(\frac{1}{x} \right)$
11. $\lim_{x \rightarrow \infty} \frac{\sqrt{x^2+1}}{x+1}$
12. $\lim_{x \rightarrow \infty} \frac{5x^3+3x^2-1}{x-4x^4}$
13. $\lim_{x \rightarrow \infty} \frac{a^x-1}{x}$
14. $\lim_{x \rightarrow \infty} \left(1 + \frac{2}{x} \right)^x$
15. $\lim_{x \rightarrow \infty} \left(1 - \frac{1}{x} \right)^x$
16. $\lim_{x \rightarrow \infty} \left(\frac{x}{1+x} \right)^x$
17. $\lim_{x \rightarrow \infty} \frac{x^4+2x^2+6}{x^2+7}$
18. $\lim_{x \rightarrow \infty} \left[\frac{x^2}{1+x} - \frac{x^2}{x+3} \right]$
19. $\lim_{x \rightarrow \infty} \left(x - \sqrt{x^2 - a^2} \right)$
20. $\lim_{x \rightarrow \infty} \frac{x^2+1}{x^{3/2}}$
21. $\lim_{x \rightarrow \infty} \frac{3-2x^4}{1+x}$
22. $\lim_{x \rightarrow -1} \frac{x^{1/3}+1}{1+x}$

$$23. \lim_{x \rightarrow 3} \left(\frac{1}{x-3} - \frac{1}{|x-3|} \right)$$

$$24. f(x) = x^2 + 3 \quad \text{if } x \leq 1$$

$$= x + 1 \quad x > 1$$

$$25. \quad = 3 \quad x \leq -2$$

$$f(x) = -\frac{1}{2}x^2 \quad -2 \leq x < 2$$

$$= 3 \quad x \geq 2$$

$$7. \ln \frac{y^2 - x^2}{y-x}$$

$$8. \ln \frac{\tan(\sin x)}{\sin x}$$

$$9. \ln x \sin \left(\frac{1}{x} \right)$$

$$10. \ln \sin \left(\frac{1}{x} \right)$$

$$11. \ln \frac{\sqrt{x^2+1}}{x+1}$$

$$12. \ln \frac{4x^3 - 2x^2}{3x^3 - 5}$$

$$13. \ln \left(1 + \frac{2}{x} \right)^x$$

$$14. \ln \left(1 + \frac{1}{x} \right)^2$$

$$15. \ln \left(\frac{x}{1+x} \right)^x$$

$$16. \ln \left(\frac{a^x - 1}{x} \right) \quad a > 1$$

$$17. \ln$$

$$\frac{x^4 - 2x^2 + 6}{x^2 + 1} \quad x \rightarrow \pi$$

$$x \rightarrow 0$$

$$18. \ln \left[\frac{x^2}{x+1} - \frac{x^2}{x+3} \right]$$

$$19. \ln \left(x - \sqrt{x^2 - a^2} \right) \quad x \rightarrow \infty$$

$$20. \ln \frac{x^2 + 1}{x^{3/2}}$$

$$21. \ln$$

$$\frac{5x^3 - 3x^2 - 1}{x - 4x^4} \quad x \rightarrow \infty$$

$$x \rightarrow \infty$$

$$x \rightarrow \infty$$

$$22. \ln \frac{3-2x^4}{1+x} \quad x \rightarrow \infty$$

$$23. \ln \frac{x^{1/3} + 1}{x+1} \quad x \rightarrow \infty$$

$$24. \ln \left(\frac{1}{x-3} - \frac{1}{|x-3|} \right) \quad x \rightarrow \infty$$

$$25. f(x) = x^2 + 3 \quad \text{if } x < 1$$

$$x+1 \quad x > 1$$

$$26. f(x) \begin{cases} 3 & x < -2 \\ -1 & -2 < x < 2 \\ 2 & x > 2 \\ 3 & \end{cases}$$

$$x \rightarrow \infty$$

Find $\lim_{x \rightarrow t} \ln x$, $\lim_{x \rightarrow -2} \ln x$, $\lim_{x \rightarrow 2} \ln x$ & $\lim_{x \rightarrow +\infty} \ln x$